

to the presence of small amounts of adsorbed gases such as nitrosyl fluoride or dinitrogen tetroxide. The bands near 3500 and 1640  $\text{cm}^{-1}$  in the spectrum of  $(\text{NO})_2\text{PtF}_6$  may be due to lattice water absorbed during the preparation of the mulls.

Other features of the spectra of these compounds were of lesser importance to the gross structural implications. That the stretching mode of the  $\text{NO}^+$  ion appeared as a doublet in  $\text{NOPtF}_6$  and  $\text{N}_2\text{O}_3\text{PtF}_6$  should probably be interpreted as being due to coupling with lattice modes. A similar interpretation is reasonable for the splitting of the  $\nu_3$  and  $\nu_1 + \nu_3$  bands of the  $\text{NO}_2^+$  ion in  $\text{N}_2\text{O}_3\text{PtF}_6$ . However, in this case the splitting might be due to different interactions between randomly oriented  $\text{NO}^+$  and  $\text{NO}_2^+$  ions in the crystal. For example, if the  $\text{NO}^+$  and  $\text{NO}_2^+$  ions lie on the major threefold axis of a structure similar to that of  $\text{O}_2\text{PtF}_6$ ,<sup>2</sup> then the three possible orientations of the ions  $\text{NO}^+—\text{NO}^+$ ,  $\text{NO}_2^+—\text{NO}_2^+$ , and  $\text{NO}^+—\text{NO}_2^+$  would result in two different crystal environments for both  $\text{NO}^+$  and  $\text{NO}_2^+$ .

**X-Ray Diffraction Results.**—The crystal data indicate that  $\text{NOPtF}_6$  is isostructural with  $\text{O}_2\text{PtF}_6$ <sup>2</sup> and  $\text{KSbF}_6$ .<sup>29</sup> These three compounds have nearly identical cell dimensions, and since the visually estimated relative intensities of  $\text{NOPtF}_6$  are very nearly the same as

those found for  $\text{O}_2\text{PtF}_6$ , the space groups for these two compounds are assumed to be identical, *i.e.*,  $T_h^4\text{-Ia}^3$ . This similarity is to be expected since the  $\text{NO}^+$  and  $\text{O}_2^+$  ions are close in size.

It has been estimated that the  $\text{NO}^+$  group, when rotating and acting as a sphere, has an effective radius of 1.40 Å,<sup>20</sup> which is close to the radius of potassium ion (1.33 Å). Since the molecular volume of  $\text{SbF}_6^-$  is nearly the same as that of the ions  $\text{OsF}_6^-$ ,  $\text{RuF}_6^-$ , and  $\text{PtF}_6^-$ ,<sup>27</sup> the isostructural relationship of  $\text{NOPtF}_6$  and  $\text{KSbF}_6$  is expected.

When the larger linear  $\text{NO}_2^+$  ion is substituted for  $\text{NO}^+$  in the crystal, the lattice expands a small amount (2.06%); this expansion is still more pronounced for  $\text{N}_2\text{O}_3^{2+}\text{PtF}_6^{2-}$  (4.64%). Although  $\text{NOPtF}_6$  and  $\text{O}_2\text{PtF}_6$  are believed to be isostructural, it cannot be determined at present whether  $\text{NO}_2\text{PtF}_6$  and  $\text{N}_2\text{O}_3\text{PtF}_6$  are also isostructural to  $\text{O}_2\text{PtF}_6$ , since the corresponding relative intensities for some reflections differ considerably. However, since these compounds are cubic, and nearly isodimensional, they probably possess closely related packing features.

**Acknowledgment.**—The authors wish to thank Dr. P. Kasai for the epr measurements and H. V. Rothman for technical assistance. Research reported in this publication was supported by the Advanced Research Projects Agency through the U. S. Army Research Office, Durham, N. C.

(29) H. Bode and E. Voss, *Z. Anorg. Allgem. Chem.*, **264**, 144 (1951).

CONTRIBUTION FROM THE REACTOR CHEMISTRY DIVISION,  
OAK RIDGE NATIONAL LABORATORY, OAK RIDGE, TENNESSEE

## The Sodium Fluoride-Lanthanide Trifluoride Systems<sup>1</sup>

By R. E. THOMA, H. INSLEY, AND G. M. HEBERT

Received January 4, 1966

Phase diagrams are reported for the  $\text{NaF-LnF}_3$  binary systems. Hexagonal phases of the formula  $\text{NaF} \cdot \text{LnF}_3$  are formed in all  $\text{NaF-LnF}_3$  systems. Above 700° the hexagonal phases  $\text{NaF} \cdot \text{PrF}_3$  to  $\text{NaF} \cdot \text{LuF}_3$  become converted to disordered fluorite-like cubic phases of variable composition. The composition limits of the cubic phase region are extended in proportion to the difference in ion size between  $\text{Na}^+$  and  $\text{Ln}^{3+}$  and vary in breadth ranging from 9 mole % ( $\text{NaF-PrF}_3$ ) to 25 mole % ( $\text{NaF-LuF}_3$ ). In each case, the  $\text{LnF}_3$ -rich phase boundary was found empirically to be  $5\text{NaF} \cdot 9\text{LnF}_3$  as the interstitial positions for anions become filled. Values of the fluorite unit-cell constants were calculated from ionic radii and found to be in good agreement with measured values. Unit-cube dimensions,  $a_0$ , range from a maximum value of 5.720 Å for the  $\text{LnF}_3$ -rich phase in the system  $\text{NaF-PrF}_3$  to 5.425 Å for the  $\text{NaF}$ -rich phase in the system  $\text{NaF-LuF}_3$ . Lattice constants for the hexagonal phases  $\text{NaF} \cdot \text{LaF}_3$  to  $\text{NaF} \cdot \text{LuF}_3$  vary for  $a_0$  from 6.157 to 5.967 Å and for  $c_0$  from 3.822 to 3.523 Å. At high temperatures the  $5\text{NaF} \cdot 9\text{LnF}_3$  phase displays disordering characteristic of the fluorite-like solid solutions; at lower temperatures cationic ordering takes place in the  $5\text{NaF} \cdot 9\text{LnF}_3$  phases where  $\text{Ln} = \text{Dy}$  to  $\text{Lu}$ , transforming the cubic phase to an orthorhombic phase. Hexagonal  $\text{NaF} \cdot \text{LnF}_3$  and orthorhombic  $5\text{NaF} \cdot 9\text{LnF}_3$  compounds are partially miscible in the solid state. In the series  $\text{Dy}$  to  $\text{Lu}$ , the hexagonal phase is increasingly soluble in  $5\text{NaF} \cdot 9\text{LnF}_3$ , stabilizing the 5:9 phase to the extent that the lutetium compound is stable at temperatures below 300°, the lower temperature limit of this study. Optical properties and refractive indices of the intermediate crystalline phases in the  $\text{NaF-LnF}_3$  systems were determined as part of this investigation. Minimum liquidus temperatures in the  $\text{NaF-LnF}_3$  systems are associated with an  $\text{NaF-NaF} \cdot \text{LnF}_3$  eutectic which varies in composition only from 25 to 29 mole %  $\text{LnF}_3$  and in temperature from 733 to 595°.

### Introduction

We proposed some time ago<sup>2</sup> that the system  $\text{NaF-YF}_3$  would serve as a model for the binary systems  $\text{Na-}$

$\text{F-SmF}_3$ ,  $-\text{EuF}_3$ ,  $-\text{GdF}_3$ ,  $-\text{TbF}_3$ ,  $-\text{DyF}_3$ ,  $-\text{HoF}_3$ ,  $-\text{ErF}_3$ ,  $-\text{TmF}_3$ ,  $-\text{YbF}_3$ , and  $-\text{LuF}_3$ . This hypothesis was based

(1) Research sponsored by the U. S. Atomic Energy Commission under contract with the Union Carbide Corp.

(2) (a) R. E. Thoma, G. M. Hebert, H. Insley, and C. F. Weaver, *Inorg. Chem.*, **2**, 1005 (1963); (b) R. E. Thoma, "Complex Compounds in the Sodium Fluoride-Rare Earth Trifluoride Systems," Proceedings of the Fourth Rare Earth Research Conference, Phoenix, Ariz., April 22-25, 1964.

on the fact that the trifluorides of the rare earths,  $\text{SmF}_3$  to  $\text{LuF}_3$ , were believed to occur in an orthorhombic form which is isomorphous with  $\text{YF}_3$ , as well as in the hexagonal form,<sup>3</sup> and that phase equilibria in the  $\text{NaF-LnF}_3$  binary systems of these lanthanides would correspond to those in  $\text{NaF-YF}_3$ , but in the systems  $\text{NaF-LaF}_3$  to  $\text{NaF-PmF}_3$  would be described qualitatively by  $\text{NaF-CeF}_3$ .<sup>4</sup> The present report records the results of attempts to test this hypothesis.

### Experimental Procedures

**Materials.**—Commercial reagent grade  $\text{NaF}$  was used for preparing all of the mixtures used in the investigation of the  $\text{NaF-LnF}_3$  systems. The lanthanide trifluorides used in this study were prepared by conversion of the appropriate oxides by ammonium bifluoride at elevated temperatures. That complete conversion to the trifluorides took place was verified by X-ray, petrographic, and chemical analysis. As previously noted,<sup>5</sup> this fluorinating agent is also effective in purifying nonvolatile fluorides and accordingly was used to ensure that fused mixtures of  $\text{NaF}$  and the lanthanide trifluorides were free of contamination by small amounts of oxides. Rare earth oxides were obtained from several vendors. With the exception of  $\text{La}_2\text{O}_3$ ,  $\text{Ce}_2\text{O}_3$ , and  $\text{Ho}_2\text{O}_3$ , the oxides were normally at least 99.99% pure with respect to the specified rare earth. All lanthanide trifluorides prepared from these oxides were analyzed at this laboratory by spectrochemical methods. The results of these analyses indicate that, although the starting materials were not as pure as claimed by the manufacturers, the concentration of contaminant cations did not exceed 0.2 atom %.

**Methods.**—Investigation of high-temperature behavior in the fluoride systems studied at this laboratory have ordinarily employed a group of standardized methods<sup>6</sup> which entail thermal analysis of crystallizing melts and subsequent thermal gradient quenching, a modification of classical quenching methods, to provide a large number of samples at a time. In the present work, very few thermal analysis data were obtained because of the ineffectiveness of this technique for the investigation of the model system  $\text{NaF-YF}_3$ .

Reactions of the  $\text{NaF-YF}_3$  cubic solid solutions could not be determined by cooling curves because little or no heat was evolved as the cubic phases nucleated; neither was their decomposition *via* solid-state reactions evident from cooling-curve data. Consequently,  $\text{NaF-LnF}_3$  equilibrium data were obtained principally from specimens which were equilibrated in a thermal gradient at temperatures ranging from 300 to 1200° (2 days to 1 month) and then quenched. The equilibration periods were varied according to the transition investigated; *e.g.*, specimens were equilibrated for 1 to 7 days if liquid-solid transitions were expected and 2 to 4 weeks if solid-state transitions were expected. In the absence of cooling-curve inflections, verification of the equilibrium phase transitions was obtained by reproducing the transition with specimens which before equilibration contained, in one case, the crystalline phase found above the transition temperature and, in the other case, the crystalline phases found below the transition temperature. Phase identification was accomplished by petrographic and X-ray diffraction analysis. X-Ray determinations of unit-cell dimensions were made with a Norelco diffractometer and  $\text{Cu K}\alpha$  radiation.

### Results

Few previous reports have recorded properties of the  $\text{NaF-LnF}_3$  systems. In general, earlier attention has

focused on investigations of the properties of hexagonal  $\text{NaF-LnF}_3$  phases.<sup>4,7-11</sup> This report describes in detail the equilibrium relationships in each  $\text{NaF-LnF}_3$  system and comprises the first extensive description of the phase diagrams of the lanthanide halide systems. The initial results obtained in the current study of the systems  $\text{NaF-SmF}_3$  to  $\text{NaF-LuF}_3$  indicated that their equilibrium behavior conformed to that predicted from the  $\text{NaF-YF}_3$  model system.<sup>2a</sup> As more complete data were obtained, however, we noted that the  $\text{NaF-YF}_3$  model was approximated only by the systems for which the  $\text{Ln}^{3+}$  and  $\text{Y}^{3+}$  radii were nearly equal and that the lanthanide group is comprised of a series of related systems, each, in general, gradually more intricate with increasing atomic number of the lanthanide. This behavior is illustrative of the prominent role of cation size in phase behavior of ionic systems and provides interesting examples of the effects caused by small changes in the size of one of the cations.

**Phase Diagrams.**—Equilibrium phase diagrams of the binary systems of sodium fluoride and the lanthanide fluorides are shown in Figure 1. The compositions and temperatures at which invariant liquid-solid equilibria occur are listed in Table I. The diagrams reported here were constructed from data obtained by the experimental procedures discussed above and on the basis of inferences drawn from observed regularities in phase transition behavior. The  $\text{NaF}$ -rich sections, for example, were based on the observed regularities in the  $\text{NaF-NaF}\cdot\text{LnF}_3$  eutectic temperatures together with interpolations and extensions of  $\text{NaF-LnF}_3$  liquidus curves reported by Cantor and Ward.<sup>12</sup> The equilibrium diagram of the system  $\text{NaF-PmF}_3$  was inferred by interpolation, because investigation was precluded by the high  $\beta$  activity of available Pm isotopes. The intent of the present study was to infer the general characteristics of the lanthanide systems on the basis of the well-established model system  $\text{NaF-YF}_3$ . Accordingly, fewer data were obtained on phase transition temperatures than have been usual in such work at this laboratory; all phase transition data obtained from thermal gradient quenching experiments are indicated on the phase diagrams (Figure 1).

Two equilibrium compounds of the formulas  $\text{NaF}\cdot\text{LnF}_3$  and  $5\text{NaF}\cdot 9\text{LnF}_3$  were observed within each of the 12  $\text{NaF-LnF}_3$  systems from  $\text{NaF-PrF}_3$  to  $\text{NaF-LuF}_3$ . Compounds of the formula  $\text{NaF}\cdot\text{LnF}_3$  occur throughout all of these systems and at temperatures below approximately 600 to 700° as hexagonal crystalline phases. At temperatures above approximately 700° these hexagonal phases are unstable. On heating, they decompose in a variety of phase reactions, differing sufficiently from each other in character and properties to enable one  $\text{NaF-LnF}_3$  system to be distinguished from another. In the systems  $\text{NaF-LaF}_3$  and  $\text{NaF-CeF}_3$  the

(3) A. Zalkin and D. H. Templeton, *J. Am. Chem. Soc.*, **75**, 2453 (1953).

(4) C. J. Barton, J. D. Redman, and R. A. Strehlow, *J. Inorg. Nucl. Chem.*, **20**, 45 (1961).

(5) R. E. Thoma, C. F. Weaver, H. A. Friedman, H. Insley, L. A. Harris, and H. A. Yakel, Jr., *J. Phys. Chem.*, **65**, 1096 (1961).

(6) H. A. Friedman, G. M. Hebert, and R. E. Thoma, "Thermal Analysis and Gradient Quenching Apparatus and Techniques for the Investigation of Fused Salt Phase Equilibria," ORNL-3373, Dec 18, 1962.

(7) W. H. Zachariasen, *J. Am. Chem. Soc.*, **70**, 2147 (1948).

(8) E. P. Dergunov, *Dokl. Akad. Nauk SSSR*, **85**, 1025 (1952).

(9) F. Mathes and S. Holz, *Z. Chem.*, **2**, 22 (1962).

(10) D. M. Roy and R. Roy, *J. Electrochem. Soc.*, **111**, 421 (1964).

(11) J. H. Burns, *Inorg. Chem.*, **4**, 881 (1965).

(12) S. Cantor and W. T. Ward, *J. Phys. Chem.*, **67**, 2766 (1963).

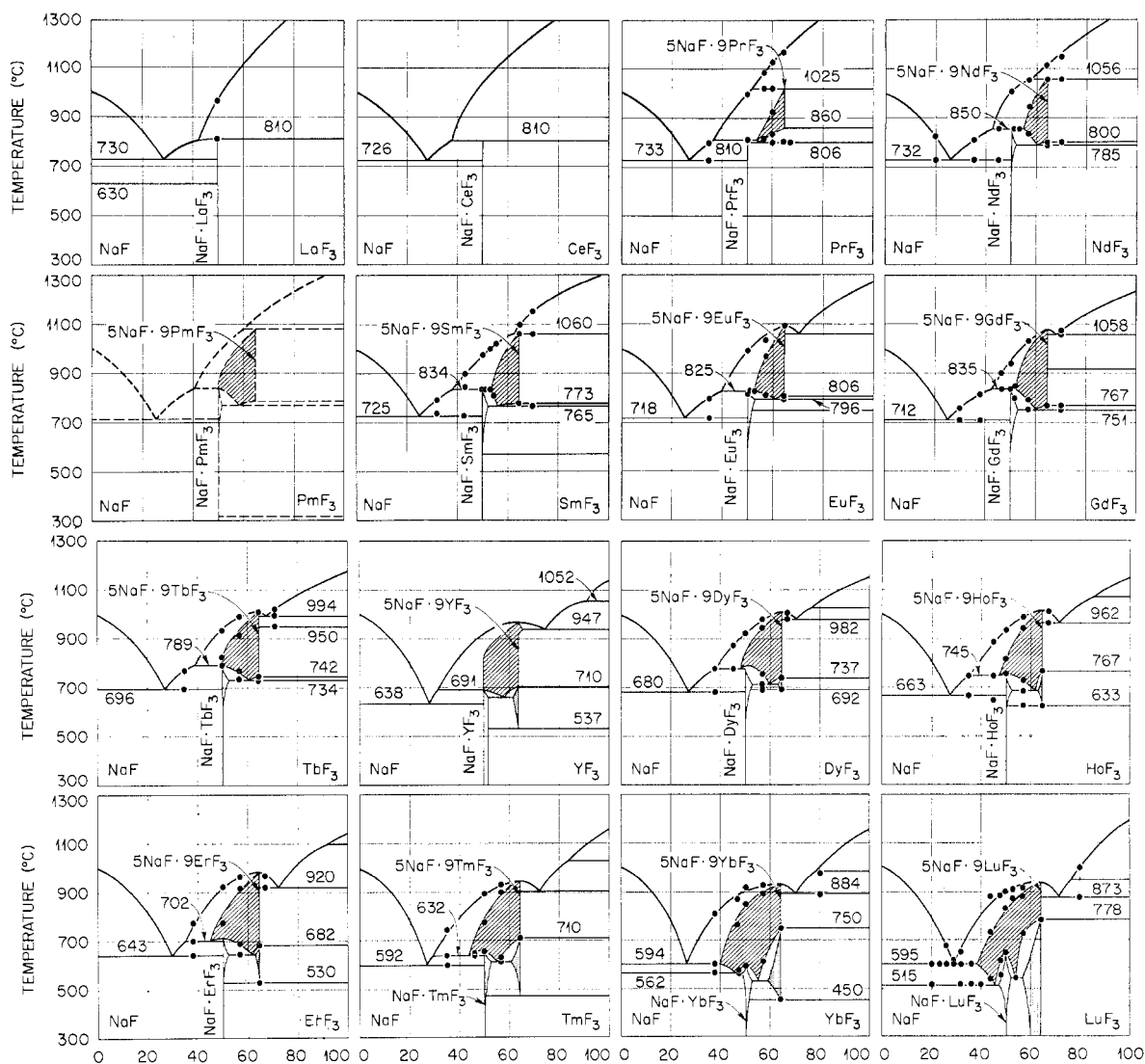


Figure 1.—Equilibrium diagrams of the NaF–LnF<sub>3</sub> systems. Diagonally hatched areas indicate cubic solid solution phases; dotted areas indicate orthorhombic phases. System NaF–CeF<sub>3</sub> from C. J. Barton, J. D. Redman, and R. A. Strehlow, *J. Inorg. Nucl. Chem.*, **20**, 45 (1961).

hexagonal phase melts incongruently to LnF<sub>3</sub> and liquid; in NaF–PrF<sub>3</sub> to NaF–GdF<sub>3</sub> it melts incongruently to a cubic fluorite-like phase and liquid, and in NaF–TbF<sub>3</sub> to NaF–LuF<sub>3</sub> it becomes disordered and inverts into the cubic phase. When formed, the cubic phase is of variable composition, qualitatively similar in its phase behavior to the corresponding phase in the NaF–YF<sub>3</sub> system. Results of the NaF–YF<sub>3</sub> investigation as well as those in the current study suggested originally that a stoichiometric cubic phase, NaF·LnF<sub>3</sub>, is an equilibrium solid in the binary systems. As compositional limits of the cubic phases in the NaF–LnF<sub>3</sub> systems were established, it became clear that equimolar stoichiometry of this phase is fortuitous. Composition limits of the cubic phases were determined from refractive index, lattice constant, and phase transition data. As in the NaF–YF<sub>3</sub> system, the upper LnF<sub>3</sub> composition limit corresponds to the compound composition 5NaF·9LnF<sub>3</sub>. The lower composition extends progressively from a limit of 55.5 mole % LnF<sub>3</sub>

to one at 39 mole % LnF<sub>3</sub> for the systems NaF–SmF<sub>3</sub> to NaF–LuF<sub>3</sub>, respectively.

Cubic NaF–LnF<sub>3</sub> phases have been observed previously by Zalkin and Templeton<sup>3</sup> and Roy and Roy.<sup>10</sup> In their determination of the structures of the rare earth trifluorides, Zalkin and Templeton observed that a cubic phase was precipitated from aqueous solutions of NaF and HoF<sub>3</sub> by HF. They inferred incorrectly that this phase was HoOF. Roy and Roy recognized the existence of some cubic NaF–LnF<sub>3</sub> phases and noted as well that they were of variable composition.

The cubic solid solution phases are unstable below temperatures varying from 800 to 530°. On cooling, they transform to a variety of products depending on the composition of the decomposing phases. At equimolar NaF–LnF<sub>3</sub> compositions, partial ordering occurs and the hexagonal NaF·LnF<sub>3</sub> phase forms. At the 5NaF·9LnF<sub>3</sub> phase boundary the cubic phase decomposes in the systems NaF–PrF<sub>3</sub> to NaF–TbF<sub>3</sub> on cooling to hexagonal NaF·LnF<sub>3</sub> and LnF<sub>3</sub>. In the systems

TABLE I

LIQUID-SOLID INVARIANT EQUILIBRIA IN THE NaF-LnF<sub>3</sub> SYSTEMS

Ln	Composition (mole % LnF <sub>3</sub> )	Temperature (°C)	Type of Equilibrium at Invariant Temperature	Equilibrium Reaction
Ln	29	730 <sup>a</sup>	Eutectic	$L \rightleftharpoons \text{NaF} + \text{hex. NaF} \cdot \text{LnF}_3$
	43	810 <sup>a</sup>	Peritectic	$L + \text{LnF}_3 \rightleftharpoons L + \text{hex. NaF} \cdot \text{LnF}_3$
Ce <sup>b</sup>	28	726	Eutectic	$L \rightleftharpoons \text{NaF} + \text{hex. NaF} \cdot \text{CeF}_3$
	38	810	Peritectic	$L + \text{CeF}_3 \rightleftharpoons L + \text{hex. NaF} \cdot \text{CeF}_3$
Pr	27	733	Eutectic	$L \rightleftharpoons \text{NaF} + \text{hex. NaF} \cdot \text{PrF}_3$
	37	810	Peritectic	$L + \text{PrF}_3 \rightleftharpoons L + \text{hex. NaF} \cdot \text{PrF}_3$
	52	1025	Peritectic	$L + \text{PrF}_3 \rightleftharpoons L + \text{cubic ss}$
Nd	26	732	Eutectic	$L \rightleftharpoons \text{NaF} + \text{hex. NaF} \cdot \text{NdF}_3$
	42	850	Peritectic	$L + \text{cubic ss} \rightleftharpoons L + \text{hex. NaF} \cdot \text{NdF}_3$
	58	1056	Peritectic	$L + \text{NdF}_3 \rightleftharpoons L + \text{cubic ss}$
Sm	25	725	Eutectic	$L \rightleftharpoons \text{NaF} + \text{hex. NaF} \cdot \text{SmF}_3$
	38	834	Peritectic	$L + \text{cubic ss} \rightleftharpoons L + \text{hex. NaF} \cdot \text{SmF}_3$
	48	1060	Peritectic	$L + \text{SmF}_3 \rightleftharpoons L + \text{cubic ss}$
Eu	25	718	Eutectic	$L \rightleftharpoons \text{NaF} + \text{hex. NaF} \cdot \text{EuF}_3$
	39	825	Peritectic	$L + \text{cubic ss} \rightleftharpoons L + \text{hex. NaF} \cdot \text{EuF}_3$
	64.3	1091	Congruent m.p.	$L \rightleftharpoons 5\text{NaF} \cdot 9\text{EuF}_3$
Gd	25	712	Eutectic	$L \rightleftharpoons \text{NaF} + \text{hex. NaF} \cdot \text{GdF}_3$
	43	810	Peritectic	$L + \text{cubic ss} \rightleftharpoons L + \text{hex. NaF} \cdot \text{GdF}_3$
	64.3	1080	Congruent m.p.	$L \rightleftharpoons 5\text{NaF} \cdot 9\text{GdF}_3$
Tb	27	696	Eutectic	$L \rightleftharpoons \text{NaF} + \text{hex. NaF} \cdot \text{TbF}_3$
	39	789	Peritectic	$L + \text{cubic ss} \rightleftharpoons L + \text{hex. NaF} \cdot \text{TbF}_3$
	64.3	1031	Congruent m.p.	$L \rightleftharpoons 5\text{NaF} \cdot 9\text{TbF}_3$
Dy	27	680	Eutectic	$L \rightleftharpoons \text{NaF} + \text{hex. NaF} \cdot \text{DyF}_3$
	38	780	Peritectic	$L + \text{cubic ss} \rightleftharpoons L + \text{hex. NaF} \cdot \text{DyF}_3$
	64.3	1020	Congruent m.p.	$L \rightleftharpoons 5\text{NaF} \cdot 9\text{DyF}_3$
Ho	27	680	Eutectic	$L \rightleftharpoons \text{NaF} + \text{hex. NaF} \cdot \text{DyF}_3$
	35	745	Peritectic	$L + \text{cubic ss} \rightleftharpoons L + \text{hex. NaF} \cdot \text{HoF}_3$
	64.3	1013	Congruent m.p.	$L \rightleftharpoons 5\text{NaF} \cdot 9\text{HoF}_3$
Er	27	643	Eutectic	$L \rightleftharpoons \text{NaF} + \text{hex. NaF} \cdot \text{ErF}_3$
	35	702	Peritectic	$L + \text{cubic ss} \rightleftharpoons L + \text{hex. NaF} \cdot \text{ErF}_3$
	64.3	975	Congruent m.p.	$L \rightleftharpoons 5\text{NaF} \cdot 9\text{ErF}_3$
Tm	27	592	Eutectic	$L \rightleftharpoons \text{NaF} + \text{hex. NaF} \cdot \text{TmF}_3$
	29	632	Peritectic	$L + \text{cubic ss} \rightleftharpoons L + \text{hex. NaF} \cdot \text{TmF}_3$
	64.3	940	Congruent m.p.	$L \rightleftharpoons 5\text{NaF} \cdot 9\text{TmF}_3$
Yb	26	594	Eutectic	$L \rightleftharpoons \text{NaF} + \text{cubic ss}$
	64.3	928	Congruent m.p.	$L \rightleftharpoons 5\text{NaF} \cdot 9\text{YbF}_3$
	70	893	Eutectic	$L \rightleftharpoons 5\text{NaF} \cdot 9\text{YbF}_3 + \text{YbF}_3$
Lu	29	595	Eutectic	$L \rightleftharpoons \text{NaF} + \text{cubic ss}$
	64.3	930	Congruent m.p.	$L \rightleftharpoons 5\text{NaF} \cdot 9\text{LuF}_3$
	72	873	Eutectic	$L \rightleftharpoons 5\text{NaF} \cdot 9\text{LuF}_3 + \text{LuF}_3$

<sup>a</sup> Eutectic and peritectic temperatures were reported by E. Mathes and S. Holz, *Z. Chem.*, **2**, 22 (1962), to be ~630 and 770°, respectively. <sup>b</sup> C. J. Barton, J. D. Redman, and R. A. Strehlow, *J. Inorg. Nucl. Chem.*, **20**, 45 (1961).

NaF-DyF<sub>3</sub> to NaF-LuF<sub>3</sub> the cubic phase again becomes partially ordered on cooling and transforms into an orthorhombic form of the compound which, except for 5NaF·9LuF<sub>3</sub>, is also unstable at lower temperatures with respect to NaF·LnF<sub>3</sub> and LnF<sub>3</sub>.

The dimensions of the crystal unit cells of the compounds observed in the NaF-LnF<sub>3</sub> systems vary monotonically with increasing atomic number of the lanthanides. Refractive indices, however, reach their maximum values for the phases in the NaF-PrF<sub>3</sub> system. Standard values for the crystallographic properties of NaF-LnF<sub>3</sub> phases, as measured in the current study, are given in Table II. These data reveal the effect of the lanthanide contraction on the crystal properties of the fluorides. Of interest is the marked effect of polarizability of lanthanide ions on refractive indices of complex compounds. As the radius of the tripositive ion decreases, refractive indices of isostructural phases also decrease, although densities of these phases increase. Levin<sup>13</sup> noted corresponding behavior in the rare earth oxides. Comparisons of refractive indices and densities of the lanthanide fluoride complex compounds and trifluorides are shown in Table II.

Optical data were obtained for the room-temperature forms of the lanthanide trifluorides, for which LaF<sub>3</sub> to SmF<sub>3</sub> are hexagonal and GdF<sub>3</sub> to LuF<sub>3</sub> are orthorhombic. Current results of an investigation of LnF<sub>3</sub> dimorphism<sup>14</sup> confirmed Zalkin and Templeton's conclu-

(13) E. M. Levin, "Refractivities of the Rare Earth Oxides," Proceedings of the Third Rare Earth Conference, Clearwater, Fla., April 21-24, 1963.

(14) G. D. Brunton and R. E. Thoma, unpublished data.

TABLE II

OPTICAL AND X-RAY POWDER DIFFRACTION DATA FOR NaF-LnF<sub>3</sub> CRYSTALLINE PHASES

Ln	Composition (mole % LnF <sub>3</sub> )	R. I.	Hexagonal NaF·LnF <sub>3</sub>			N <sub>c</sub>	N <sub>w</sub>	
			a <sub>0</sub> (Å)	c <sub>0</sub> (Å)	σ(c <sub>0</sub> )			
Ln	29	730 <sup>a</sup>	6.147	0.006	3.822	0.008	1.486	1.500
Ce	28	726	6.131	0.006	3.776	0.004	1.493	1.514
Pr	38	810	6.123	0.004	3.743	0.002	1.494	1.516
Nd	52	1025	6.100	0.002	3.711	0.002	1.493	1.515
Pm	(6.056)	-	(3.670)	-	-	-	(1.492)	(1.515)
Sm	6.051	0.010	3.640	0.007	1.492	1.516		
Eu	6.044	0.603	3.613	0.003	1.492	1.516		
Gd	6.020	0.003	3.601	0.008	1.483	1.507		
Tb	6.008	0.004	3.580	0.002	1.486	1.506		
Dy	5.985	0.004	3.554	0.003	1.486	1.510		
Ho	5.991	0.001	3.528	0.002	1.486	1.510		
Er	5.950	0.002	3.514	0.002	1.482	1.504		
Tm	5.953	0.002	3.494	0.002	1.476	1.495		
Yb	5.929	0.002	3.471	0.002	1.482	1.504		
Lu	5.912	0.003	3.458	0.003	1.484	1.506		
(Y)	5.967	0.002	3.523	0.002	1.464	1.486		

B. Cubic NaF·LnF <sub>3</sub> Phases at Composition Limits						
Ln	Composition (mole % LnF <sub>3</sub> )	R. I.	a <sub>0</sub> (Å)	X-Ray Density (g/cc)	5NaF·9LnF <sub>3</sub> Composition Limit	
					R. I.	a <sub>0</sub> (Å)
Ln	29	730	3.572	5.766		
Pr	55.5	1.512	5.710	5.962		
Nd	55.0	1.506	5.670	6.131		
Pm	(54.5)	(1.500)	(5.630)	(4.620)	(1.522)	(5.655)
Sm	53.5	1.495	5.605	4.702	1.520	5.627
Eu	52.5	1.486	5.575	4.809	1.519	5.616
Gd	51.5	1.470	5.550	4.978	1.502	5.594
Tb	50.0	1.472	5.535	5.051	1.504	5.565
Dy	48.5	1.462	5.505	5.205	1.504	5.547
Ho	47.0	1.458	5.490	5.296	1.504	5.525
Er	45.0	1.440	5.475	5.387	1.493	5.514
Tm	43.5	1.427	5.460	5.466	1.494	5.493
Yb	41.5	1.415	5.440	5.611	1.488	5.480
Lu	39.0	1.402	5.425	5.698	1.482	5.463

C. Orthorhombic 5NaF·9LnF <sub>3</sub>								
Ln	Composition (mole % LnF <sub>3</sub> )	R. I.	Refractive Index			Lattice Constants (Å)		
			N <sub>x</sub>	N <sub>y</sub>	N <sub>mean</sub>	a <sub>0</sub>	b <sub>0</sub>	c <sub>0</sub>
Ln	29	730	1.514	1.547	1.532	39.23	7.845	
Dy	48.5	1.462	1.510	1.525	1.518	39.07	7.814	
Ho	47.0	1.458	1.506	1.514	1.510	38.99	7.798	
Er	45.0	1.440	1.501	1.493	1.497	38.84	7.768	
Yb	41.5	1.415	1.495	1.480	1.487	38.75	7.750	
Lu	39.0	1.402	1.487	1.487	1.487	38.63	7.725	

D. Hexagonal and Orthorhombic LnF <sub>3</sub>									
Ln	Symmetry	Refractive Index			Lattice Constants (Å)			Density (g/cc)	Reference
		N <sub>x</sub>	N <sub>y</sub>	N <sub>z</sub>	a <sub>0</sub>	b <sub>0</sub>	c <sub>0</sub>		
La	Hexagonal	1.597	1.603	1.603	7.186	-	7.352	5.936	a
Ce	Hexagonal	1.607	1.613	1.613	7.112	-	7.279	6.157	b
Pr	Hexagonal	1.614	1.618	1.618	7.075	-	7.238	6.14	c
Nd	Hexagonal	1.621	1.628	1.628	7.030	-	7.200	6.506	a
Sm	Orthorhombic	1.577	1.608	1.608	6.669	7.059	4.405	6.643	a
Eu	Orthorhombic	1.572	1.600	1.600	6.622	7.019	4.396	6.793	d
Gd	Orthorhombic	1.570	1.600	1.600	6.571	6.985	4.393	7.056	e
Tb	Orthorhombic	1.570	1.600	1.600	6.513	6.949	4.384	7.236	e
Dy	Orthorhombic	1.570	1.600	1.600	6.460	6.906	4.376	7.465	e
Ho	Orthorhombic	1.566	1.598	1.598	6.404	6.875	4.379	7.644	e
Er	Orthorhombic	1.566	1.598	1.598	6.354	6.848	4.380	7.814	e
Tm	Orthorhombic	1.564	1.598	1.598	6.283	6.811	4.408	7.971	e
Yb	Orthorhombic	1.558	1.568	1.568	6.236	6.766	4.434	8.164	e
Lu	Orthorhombic	1.554	1.558	1.558	6.181	6.731	4.446	8.44	-

<sup>a</sup> E. Staritzky and L. B. Aspree, *Anal. Chem.*, **29**, 857 (1957).

<sup>b</sup> ASTM X-Ray Diffraction Card No. 8-45. <sup>c</sup> ASTM X-Ray Diffraction Card No. 6-0325. <sup>d</sup> A. Zalkin and D. H. Templeton, *J. Am. Chem. Soc.*, **75**, 2453 (1953). <sup>e</sup> ASTM X-Ray Diffraction Card No. 12-788.

sion that the hexagonal form of the heavier lanthanides is the high-temperature modification. The NaF-LnF<sub>3</sub> phase diagrams reported here are drawn so as to indicate the hexagonal-orthorhombic inversion.

A salient feature of the NaF-LnF<sub>3</sub> systems is the unusual behavioral sequence produced by the compositional variability of the fluorite-like phases. This behavior shows the remarkable effect of cation size and polarizability in lanthanide systems. As shown in Figure 1, the cubic phase is not formed at all in the systems NaF-LaF<sub>3</sub> and NaF-CeF<sub>3</sub>, is formed by NaF and PrF<sub>3</sub>, and is extended to an increasingly broad composition range throughout the rest of the system sequence. That equilibrium occurrence of the compositionally variable cubic phase is a size-related phenomenon and is not restricted to the lanthanide- or NaF-based systems was verified by tests with binary mix-

tures of NaF-BiF<sub>3</sub> and KF-LaF<sub>3</sub>, whose Na<sup>+</sup>:M<sup>3+</sup> cation radius ratios, 1.05 and 1.25, are comparable to those of the NaF-LnF<sub>3</sub> pairs. In both systems hexagonal and cubic analogs of the NaF-LnF<sub>3</sub> phases were observed.

Previously, it was noted that a solid phase occasionally was nucleated metastably<sup>2a</sup> when NaF-YF<sub>3</sub> melts containing 35 to 40 mole % YF<sub>3</sub> were rapidly cooled. The phase was found to be metastable with respect to the equilibrium solids NaF and NaF·YF<sub>3</sub>. In the present investigation a corresponding phase was found to form metastably in the NaF-ErF<sub>3</sub> to NaF-LuF<sub>3</sub> systems. Its formula is tentatively regarded as 5NaF·3LnF<sub>3</sub>. Crystals of the YF<sub>3</sub> member have been indexed as orthorhombic,<sup>15</sup> with lattice constants  $a_0 = 6.24$ ,  $b_0 = 3.88$ , and  $c_0 = 5.82$  Å, and have a mean refractive index of 1.422.

In attempts to produce the hexagonal form of NaF·LuF<sub>3</sub>, we found that this phase was difficult to nucleate because of the slow transformation rate of the cubic solid solution phase. As the cubic phase transformed partially to the hexagonal NaF·LuF<sub>3</sub>, we found that at least one metastable solid phase was formed during the process. Because the metastable material was poorly crystallized and of low symmetry, it was not possible to ascertain whether one or more discrete phases were formed.

Apart from the formation of the nonequilibrium solids described above, metastable nucleation in the NaF-LnF<sub>3</sub> systems was not noted. The solid-state transformations require long periods for equilibrium to be attained, but, in general, proceed without generating metastable phases.

Several trends are developed in the NaF-LnF<sub>3</sub> systems as Na<sup>+</sup>:Ln<sup>3+</sup> size disparity increases and as tripositive ion polarizability decreases. As predicted,<sup>16</sup> there is a marked tendency for the total number of intermediate crystal phases produced by the interactions of a given NaF-LnF<sub>3</sub> component pair to increase throughout the series. A trend also develops toward broadening the composition limits and extension of the temperature range through which the cubic and orthorhombic phases are stable. The trends toward increasing number, compositional variability, and stability of the NaF-LnF<sub>3</sub> crystal phases appear to be distinct, not only with respect to the crystal chemistry of the complex compounds but also in their modes of crystallization from molten mixtures. The cubic solid solution phase, for example, has no equilibrium stability below approximately 500° with respect to the hexagonal NaF·LnF<sub>3</sub> and LnF<sub>3</sub> phases but is increasingly easier to retain metastably in cooled melts of appropriate compositions in the system group NaF-DyF<sub>3</sub> to NaF-LuF<sub>3</sub>. This tendency is so marked that in the NaF-LuF<sub>3</sub> system the cubic phase can be crystallized from the melt even under slow-cooling conditions. These trends are believed to be indicative of an increase in the lattice energies of the crystalline phases resulting from the lan-

thanide contraction and of a corresponding decrease in polarizability. The decrease in polarizability is probably the most influential factor in enabling compositional variability of the phases to be extended with increasing atomic number of the lanthanide. The more polarized ions of the lighter lanthanides should tend to form crystalline phases of fixed stoichiometry, while the less polarized ions, by being more electronically symmetrical and of smaller size than Na<sup>+</sup>, should exhibit less selectivity for given whole-number stoichiometric ratios. The vertical phase boundary at the 5-NaF·9LnF<sub>3</sub> composition represents LnF<sub>3</sub> saturation of the fluorite-like phase. Presumably, the equimolar composition represents a packing limit for Na<sup>+</sup> in hexagonal NaF·LnF<sub>3</sub> as well. Considered as resulting directly from size and polarizability factors, the trends in the NaF-LnF<sub>3</sub> systems, as discussed above, appear to be surprising chiefly in the gross influence these factors play in affecting phase behavior and crystal chemistry.

Size factors alone dictate that fluorite-like phases should also be found in the actinide systems NaF-UF<sub>3</sub> and NaF-PuF<sub>3</sub>, where, in fact, no such phases have been observed. The absence of cubic phases in the actinide systems may be attributed to polarizability of the actinide ions. As evidenced by trends in the molar refractivities of the lanthanide and actinide fluoride compounds, reduction in polarizability of the actinides corresponding to that in the lanthanides is not manifest. Molar refraction of NaF-LnF<sub>3</sub> crystalline phases decreases approximately 20% across the lanthanide series with increasing *Z*. Data are not available for comparison with analogous actinide phases. However, the calculated values of molar refraction for the three actinide compounds 2RbF·ThF<sub>4</sub>, 2RbF·UF<sub>4</sub>, and 2RbF·AmF<sub>4</sub> are 26.50, 32.27, and 28.98 cc, respectively. We infer from the trend in these values that reduction in polarizability of the trivalent actinide ions does indeed occur with increasing atomic number but that the decrease begins with the series rather than initially as in the rare earth group. Assuming that polarizability of the heavy-metal ions influences formation of the cubic phase in a significant way, it is anticipated that such phases will occur with the heavier actinides. Comparisons of the available information on the trifluoride systems of the lanthanides and actinides indicate that, although the systems are not exact analogs, they are sufficiently similar to permit qualitative estimates concerning the characteristics of the sodium fluoride-actinide trifluoride systems. The fact, for example, that all of the sodium fluoride-heavy metal trifluoride systems in the Na<sup>+</sup>:M<sup>3+</sup> cation size ratio 0.93 to 1.21, including all of the NaF-LnF<sub>3</sub> systems, NaF-BiF<sub>3</sub>, NaF-UF<sub>3</sub>, and NaF-PuF<sub>3</sub>, form the hexagonal NaF-MF<sub>3</sub> phase indicates that this phase is to be expected throughout the sodium fluoride-actinide trifluoride series.

**Crystal Structures.**—Three types of equilibrium crystalline phases are produced from the reactions of NaF with the lanthanide trifluorides, a hexagonal NaF·LnF<sub>3</sub> phase, a compositionally variable high-tempera-

(15) J. H. Burns, unpublished data.

(16) R. E. Thoma, *Inorg. Chem.*, **1**, 220 (1962).

ture cubic phase, and an orthorhombic  $5\text{NaF}\cdot 9\text{LnF}_3$  phase. In addition, two metastable solids have been observed: an orthorhombic phase,  $5\text{NaF}\cdot 3\text{LnF}_3$ , and an  $\text{NaF}\cdot \text{LnF}_3$  phase of low but unknown symmetry. Structural studies of the equilibrium solids show that in all  $\text{NaF}\text{-LnF}_3$  crystal phases the cation lattices are partially or extensively disordered. For systems in which the  $\text{Na}^+:\text{Ln}^{3+}$  cation ratio is unity or slightly less, entropy-related disordering at elevated temperatures is great, and the least ordered crystalline solids, the cubic and orthorhombic phases, do not form. The trend toward their formation as cation size disparity increases is evident in Figure 1.

**Hexagonal  $\text{NaF}\text{-LnF}_3$  Compounds.**—The crystal structure of  $\text{NaF}\cdot \text{NdF}_3$  was described by Burns<sup>11</sup> as consisting of an ordered array of  $\text{F}^-$  ions interspersed with cations on three types of sites. Two-thirds of the  $\text{Nd}^{3+}$  ions occupy one kind of site; one-third of the  $\text{Na}^+$  ions are randomly mixed in a second site; and two-thirds of the  $\text{Na}^+$  ions are randomly distributed with vacancies on a third kind of site. Examination of single crystals of this phase containing each of the lanthanides (except Yb and Lu) and Y showed them to be essentially isostructural. A change in space group, observed in some cases, was attributed to intermixing of cations between the first two kinds of sites.<sup>11</sup> We have made X-ray powder diffractometric measurements of the entire series of compounds and have obtained refined lattice parameters by least squares. The results are shown in Table II. Some of the compounds were measured previously by Roy and Roy;<sup>10</sup> our values are in agreement with theirs.

**Cubic  $\text{NaF}\text{-LnF}_3$  Compounds.**—The structure of  $\text{NaYF}_4$ , established by Hund,<sup>17</sup> is typical of the cubic form of  $\text{NaF}\text{-LnF}_3$  cubic phases. It is of the  $\text{CaF}_2$  (fluorite) type (Figure 2), with the  $\text{Ca}^{2+}$  ionic sites randomly occupied by  $\text{Na}^+$  and  $\text{Ln}^{3+}$  ions. The isomorphism of the high-temperature  $\text{NaF}\text{-LnF}_3$  cubic phases with  $\text{NaYF}_4$ , for  $\text{Ln} = \text{Nd}$  to  $\text{Lu}$ , has been determined by X-ray powder diffraction; values for  $a_0$  at equimolar compositions are given in Figure 3, and  $a_0$  values at the phase composition limits are given in Table II.

For this structure the unit-cube dimension can be calculated from the ionic radii.<sup>18</sup> Fair agreement between observed and calculated lattice constants, Figure 3, is achieved if the radius,  $r(\text{Na}, \text{Ln})$ , of the ion is assumed to have the following values: for  $r(\text{Ln}) > r(\text{Na})$ ,  $r(\text{Na}, \text{Ln}) = r(\text{Ln})$ , and for  $r(\text{Ln}) < r(\text{Na})$ ,  $r(\text{Na}, \text{Ln}) = \frac{1}{2}[r(\text{Ln}) + r(\text{Na})]$ . The use of these radii is rationalized by noting that, when  $r(\text{Ln}) > r(\text{Na})$ , the repulsion of the trivalent ions keeps them at equilibrium distances much as if the Na ions were not present, while, for  $r(\text{Na}) > r(\text{Ln})$ , the larger Na ion is compressed by the  $\text{Ln}\text{-F}$  attractive forces to the extent that an average cation radius is attained. Thus, because of the disorder among the cations, the lanthanide con-

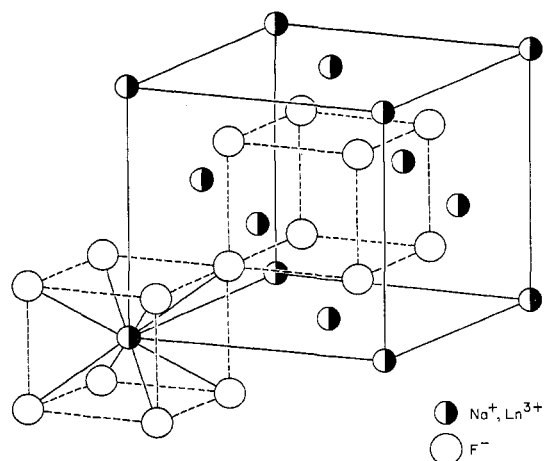


Figure 2.—Structure of cubic  $\text{NaLnF}_4$ . Equal numbers of  $\text{F}^-$  cubes (dotted lines) contain cations and vacancies.

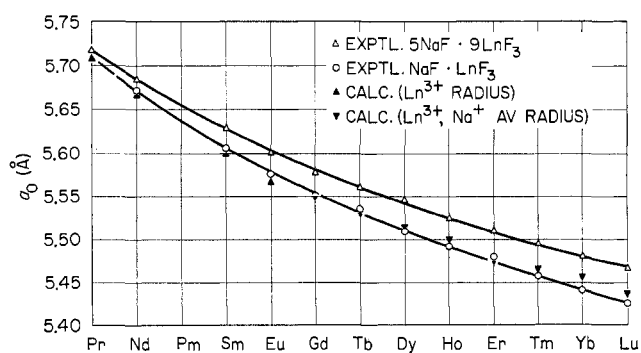


Figure 3.—Unit-cell constants of  $\text{NaF}\text{-LnF}_3$  and  $5\text{NaF}\cdot 9\text{LnF}_3$ .

traction is less pronounced in the present group than would be the case in a comparable isomorphous series of ordered crystals.

In the fluorite structure each cation, such as the one at the origin of the unit cell, Figure 2, is coordinated by a cube of  $\text{F}^-$  ions, but, for each cube with a cation at its center, there is another which is empty, such as the one at the center of the unit cell. It was shown by Hund<sup>19</sup> that the solution of  $\text{YF}_3$  in cubic  $\text{NaYF}_4$  occurs by substituting  $\text{Y}^{3+}$  for  $\text{Na}^+$  ions and by filling some of the vacancies with  $\text{F}^-$  ions to produce electroneutrality. We have found that the limit of substitution is at the composition  $5\text{NaF}\cdot 9\text{YF}_3$  and that this phase region exists in all of the  $\text{NaF}\text{-LnF}_3$  systems which contain a fluorite-like phase. The unit-cell constants for these compounds are given in Table II and Figure 3. Their larger values relative to the corresponding  $\text{Na}\text{-LnF}_4$  compounds are due to the lattice stuffing.

As represented by the Lorentz-Lorenz equation, molar refraction approximates the volume occupied by the constituent ions in crystalline phases. A measure of the crystal free space can therefore be estimated from the difference between molar volume, as computed from unit-cell dimensions, and the molar refraction. As the atomic number increases, small increases in the free space fraction are noted for the lanthanide trifluorides and for hexagonal  $\text{NaF}\cdot \text{LnF}_3$  phases (Table III). A more pronounced increase in free space fraction is found

(17) F. Hund, *Z. Anorg. Allgem. Chem.*, **261**, 106 (1950).

(18) D. H. Templeton and C. H. Dauben, *J. Am. Chem. Soc.*, **76**, 5237 (1954).

(19) F. Hund, *Z. Anorg. Allgem. Chem.*, **263**, 102 (1950).

TABLE III  
 MOLAR VOLUMES AND FREE SPACE FOR SOME  $\text{LnF}_3$  COMPOUNDS

	La	Ce	Pr	Nd	Sm	Eu	Gd	Tb	Dy	Ho	Er	Tm	Yb	Lu
A. Lanthanide Trifluorides														
U.C.V. <sup>a</sup>	54.79	53.14	52.29	51.36	51.85	51.08	50.40	49.60	48.80	48.20	47.63	47.15	46.75	46.43
M.V. <sup>b</sup>	33.00	32.01	31.49	30.93	31.23	30.77	30.36	29.87	29.39	29.03	28.69	28.40	28.16	27.30
M.R. <sup>c</sup>	11.30	11.10	10.90	10.70	10.36	10.20	10.00	9.80	9.62	9.45	9.25	9.06	8.88	8.68
M.F.S. <sup>d</sup>	21.70	20.91	20.59	20.21	20.87	20.57	20.36	20.07	19.77	19.58	19.44	19.34	19.28	18.62
% F.S. <sup>e</sup>	65.76	65.32	65.39	65.34	66.83	66.85	67.06	67.19	67.27	67.44	67.76	68.10	68.47	68.20
B. Tetragonal $\text{LiF}\cdot\text{LnF}_3$														
U.C.V.	-	-	-	-	-	74.78	74.65	73.33	72.79	71.56	71.24	70.54	69.95	69.41
M.V.	-	-	-	-	-	45.04	44.96	44.17	43.84	43.10	42.91	42.49	42.13	41.81
M.R.	-	-	-	-	-	12.87	12.78	12.64	12.57	12.28	12.24	12.05	11.91	11.79
M.F.S.	-	-	-	-	-	32.07	32.18	31.53	31.27	30.82	30.67	30.44	30.22	30.02
% F.S.	-	-	-	-	-	71.20	71.57	71.38	71.32	71.50	71.47	71.64	71.73	71.80
C. Hexagonal $\text{NaF}\cdot\text{LnF}_3$														
U.C.V.	83.65	81.94	80.76	79.72	76.73	76.19	75.34	74.60	73.49	73.10	72.04	71.48	70.44	69.77
M.V.	50.38	49.35	48.64	48.02	46.21	45.89	45.38	44.93	44.26	44.03	43.39	43.05	42.43	42.02
M.R.	14.65	14.55	14.45	14.25	13.72	13.55	13.25	13.15	12.98	12.92	12.60	12.45	12.18	12.05
M.F.S.	35.73	34.80	34.19	33.77	32.49	32.34	32.12	31.78	31.28	31.11	30.79	30.60	30.25	29.97
% F.S.	70.92	70.52	70.29	70.33	70.31	69.00	70.78	70.73	70.67	70.65	70.96	71.08	71.29	71.32
D. Cubic $\text{NaF}\cdot\text{LnF}_3$ (Equimolar) s.s.														
U.C.V.	-	-	-	-	-	-	-	84.78	83.41	82.73	82.06	81.39	80.49	79.83
M.V.	-	-	-	-	-	-	-	51.06	50.24	49.83	49.42	49.02	48.48	48.08
M.R.	-	-	-	-	-	-	-	14.11	13.85	13.51	13.20	12.89	12.71	12.46
M.F.S.	-	-	-	-	-	-	-	36.95	39.39	46.32	36.22	36.11	35.77	35.62
% F.S.	-	-	-	-	-	-	-	72.36	72.43	72.89	73.29	73.66	73.78	74.08
E. Cubic $5\text{NaF}\cdot 9\text{LnF}_3$														
U.C.V.	-	-	-	-	-	-	-	86.17	85.34	84.33	83.82	82.87	82.28	81.52
M.V.	-	-	-	-	-	-	-	51.90	51.40	50.79	50.49	49.91	49.56	49.10
M.R.	-	-	-	-	-	-	-	18.77	18.60	18.24	17.98	17.59	17.50	17.35
M.F.S.	-	-	-	-	-	-	-	33.13	32.63	32.59	32.51	32.32	32.06	31.75
% F.S.	-	-	-	-	-	-	-	63.83	63.48	64.17	64.39	64.76	64.69	64.66

<sup>a</sup> Unit-cell volume ( $\times 10^{-24}$  cm<sup>3</sup>). <sup>b</sup> Molar volume (cm<sup>3</sup>). <sup>c</sup> Molar refraction (cm<sup>3</sup>). <sup>d</sup> Molar free space (cm<sup>3</sup>). <sup>e</sup> % free space.

for the fluorite-like  $\text{NaF}\cdot\text{LnF}_3$  phases, with an even greater increase in the free space fraction for the equimolar cubic phases than for the cubic  $5\text{NaF}\cdot 9\text{LnF}_3$  phases as  $Z$  increases. Substitutional solution of  $\text{Ln}^{3+}$  into the fluorite unit cell gives rise to cation vacancies but is partly compensated for by the filling of interstitial positions with fluoride ions as described by Roy and Roy.<sup>10</sup> The fact that the space fraction occupied by the ions in the cubic structure at the  $5\text{NaF}\cdot 9\text{LnF}_3$  saturation limit is greater than at the equimolar composition lends additional evidence to the validity of the interstitial fluorine model for solution mechanism. We conclude that the combined effect of the reduction in polarizability of the lanthanide ions and the increase in free space within the crystal lattice is to reduce the specificity of  $\text{Na}^+$  and  $\text{Ln}^{3+}$  ions with regard to the cation sites they occupy in fluorite-like, orthorhombic, and hexagonal crystals. The consequence of this effect is thereby to increase the compositional variability of the crystal phases observed in the  $\text{NaF}\cdot\text{LnF}_3$  systems with increasing atomic number of the lanthanide.

**Orthorhombic  $5\text{NaF}\cdot 9\text{LnF}_3$  Compounds.**—As temperature is lowered, the cubic phases  $5\text{NaF}\cdot 9\text{LnF}_3$  to  $5\text{NaF}\cdot 9\text{LuF}_3$  undergo a solid-state transition and invert from cubic to orthorhombic symmetry. The low-temperature modification exhibits an X-ray diffraction powder pattern which is consistent with a cubic unit cell of approximately the same dimension as that of the high-temperature form, but the space lattice has changed from face-centered to primitive. In this form the cations have segregated into definite crystallographic sites, thus lowering the symmetry. Incomplete results of a

current investigation of single crystals of orthorhombic  $5\text{NaF}\cdot 9\text{LuF}_3$ <sup>20</sup> show that the diffraction symmetry of  $5\text{NaF}\cdot 9\text{LuF}_3$  is  $\text{Cmmm}$ . The space groups consistent with this diffraction symmetry are  $\text{Cmmm}$ ,  $\text{C222}$ , and  $\text{Cmm2}$  or the other axial variations of  $\text{Cmm2}$ . The orthorhombic cell has dimensions obtained in measurements of the single crystals:  $a = 7.74$ ,  $b = 38.5$ , and  $c = 5.52$  Å. Ideally, the relationships among the unit-cell dimensions are such that  $a = \sqrt{2}c$  and  $b = 5\sqrt{2}c$ . Since  $c$  has the value of the fluorite-cell parameter, it is not unreasonable to expect that the fluorite structure remains and the eight anions surround the cation sites as in that structure. The orthorhombic symmetry and the long dimensions of the unit-cell parameters are then caused by an ordering of the cations.

**Phase Change and Structure.**—Some of the features of the  $\text{NaF}\cdot\text{LnF}_3$  phase diagrams can be explained from a crystal-chemical viewpoint. At the higher temperatures the fluorite-like phase occurs (for  $\text{Ln} = \text{Nd}$  to  $\text{Lu}$ ) with randomized distribution of cations on certain sites. The eight-coordinated holes can accommodate  $\text{F}^-$  ions to a certain extent, so that substitutional (cation) and interstitial (anion) solid solution occurs to a limit of  $5\text{NaF}\cdot 9\text{LnF}_3$ . As the temperature is lowered, differently charged and sized cations tend to find different environments and, hence, to segregate. At least three recognizable influences are considered as contributory to the solid-state phase behavior involving the cubic, hexagonal, and orthorhombic phases. As

(20) H. Steinflink, University of Texas, and G. D. Brunton, Oak Ridge National Laboratory, unpublished results, 1964.

temperature is lowered, the kinetic energy is lowered and there is greater tendency for ordering of the cations resulting in the separation of crystalline phases with definite stoichiometry. Cooling NaF-LnF<sub>3</sub> mixtures reflects this tendency by exhibiting the exsolution behavior which occurs as is indicated by the lower temperature phase boundary of the cubic phase. A somewhat opposite tendency is introduced as the reduction in polarizability of the lanthanide (with increasing atomic number of Ln) tends to allow increasing compositional variability in the low-temperature hexagonal and orthorhombic crystalline phases.

**Stoichiometry of 5Na·9LnF<sub>3</sub>.**—The formula of this phase has been established by entirely empirical

microscopic and X-ray diffraction analytical methods which are considered to be accurate within  $\pm 0.5$  mole %. Investigation of the structure of the orthorhombic form of the compound has not yet advanced to the point that the exact stoichiometry is certain. Accordingly, confirmation of the formula of this compound necessitates completion of the structural investigation currently in progress.

**Acknowledgments.**—The authors wish to express gratitude to their associates J. H. Burns and G. D. Brunton for contributions toward elucidation of the phenomena described in the present report and to J. E. Ricci for valuable discussions.

CONTRIBUTION FROM THE DEPARTMENT OF CHEMISTRY,  
THE UNIVERSITY, SHEFFIELD 10, UNITED KINGDOM

## Contrasting Behavior of Boron Trifluoride and Phosphorus Pentafluoride toward Sulfolane<sup>1</sup>

By JOHN G. JONES<sup>2</sup>

Received November 22, 1965

Sulfolane forms a 1:1 complex with boron trifluoride. The complex has  $\delta^{19}\text{F} = +144.1$  ppm ( $\delta$  relative to CCl<sub>3</sub>F) and  $\delta^{11}\text{B} = +19.2$  ppm ( $\delta$  relative to trimethyl borate). In contrast to this, sulfolane forms no stable solid complex with phosphorus pentafluoride, though the <sup>19</sup>F resonance shows evidence of interaction and of P-F bond breaking.

### Introduction

Sulfolane has been found to be a good aprotic solvent, dissolving molecular and ionic substances<sup>3</sup> without being attacked by even such strongly reactive species as the nitronium ion.<sup>4</sup> In this laboratory it has been used for nmr studies of pyridine-Lewis acid adducts<sup>5</sup> because its very low proton basicity ( $\text{p}K_{\text{BH}^+} = -12.88$ )<sup>6</sup> suggested that it might be a very weak Lewis base, unable to displace a strong base, such as pyridine, from its adducts with Lewis acids.

However, despite some reported failure<sup>7</sup> to prepare adducts of Lewis acids with sulfones, Lindqvist and Einarsson<sup>8a</sup> have prepared solid adducts of dimethyl and diphenyl sulfones with antimony tri- and pentachloride, the structure of Me<sub>2</sub>SO<sub>2</sub>·SbCl<sub>5</sub> having been determined,<sup>8b</sup> and Langford and Langford<sup>9</sup> succeeded

in preparing weak hygroscopic complexes of sulfolane itself with anhydrous cobalt(II) salts. More recently Laughlin<sup>10</sup> has found that 1 mole of methyl *n*-dodecyl sulfone dissolved in benzene would take up 1 mole of boron trifluoride, though he could isolate no solid complex, and Drago, *et al.*,<sup>11</sup> found spectroscopic evidence for charge-transfer interaction with iodine. Lastly, in a footnote, Alder and Whiting<sup>12</sup> observed that sulfolane and boron trifluoride react to give a solid product.

These findings suggested that although sulfones are such weak Brønsted bases that they are not protonated in 100% H<sub>2</sub>SO<sub>4</sub>, they may be good Lewis bases. Accordingly, it was decided to investigate the action of boron trifluoride and phosphorus pentafluoride on sulfolane.

### Experimental Section

Sulfolane (kindly supplied by the Shell Chemical Co., Shell Center, London S.E.1, U. K.) was purified in 500-ml batches by first treating with 25 ml of "100 volume" hydrogen peroxide and 25 ml of 96% H<sub>2</sub>SO<sub>4</sub>, which together oxidize any sulfoxide present. The remaining hydrogen peroxide and water were distilled off under vacuum and then the main body of solvent was collected by vacuum distillation, bp 90–100° (4–7 mm), dry nitrogen being passed through the vacuum leak. This sulfolane, now water-

- (1) Tetrahydrothiophene 1,1-dioxide; tetramethylene sulfone.
- (2) ICI Research Fellow. This work was supported by the University of Sheffield. Thanks are expressed to the Shell Chemical Co. for a gift of sulfolane.
- (3) R. S. Drago in "Non-Aqueous Solvent Systems," T. C. Waddington, Ed., Academic Press Inc., New York, N. Y., 1965.
- (4) (a) S. J. Kuhn and G. A. Olah, *J. Am. Chem. Soc.*, **83**, 4564 (1961); (b) J. Jones and J. Jones, *Tetrahedron Letters*, **31**, 2117 (1964).
- (5) J. G. Jones, Abstracts of Chemical Society (London), Anniversary Meetings, Glasgow, 1965, p X8.
- (6) S. K. Hall and E. A. Robinson, *Can. J. Chem.*, **42**, 113 (1964).
- (7) F. A. Cotton and R. Francis, *J. Am. Chem. Soc.*, **82**, 2986 (1960).
- (8) (a) T. Lindqvist and P. Einarsson, *Acta Chem. Scand.*, **13**, 420 (1959); (b) quoted by Lindqvist in "Inorganic Adduct Molecules of Oxo-Compounds," Springer-Verlag, Berlin, 1963.
- (9) C. H. Langford and P. O. Langford, *Inorg. Chem.*, **1**, 184 (1962).

- (10) R. G. Laughlin, *J. Org. Chem.*, **25**, 864 (1960).
- (11) R. S. Drago, B. Wayland, and R. L. Carlson, *J. Am. Chem. Soc.*, **85**, 3125 (1963).
- (12) R. W. Alder and M. C. Whiting, *J. Chem. Soc.*, 4707 (1964).